

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

9063352144

FURTHER MATHEMATICS

9231/32

Paper 3 Further Mechanics

May/June 2024

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

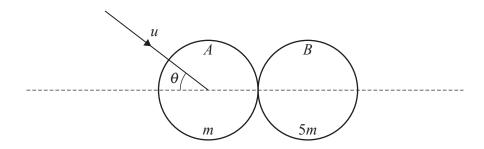
INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use $10 \,\mathrm{m\,s^{-2}}$.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages.



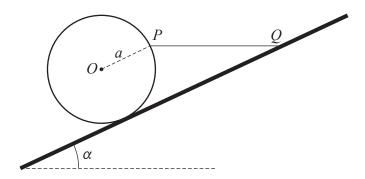
Two smooth uniform spheres A and B of equal radii have masses m and 5m respectively. Sphere A is moving on a smooth horizontal surface with speed u when it collides with sphere B which is at rest on the surface. Immediately before the collision, A's direction of motion makes an angle of θ with the line of centres. After the collision, the kinetic energies of A and B are equal. The coefficient of restitution between the spheres is $\frac{1}{2}$.

Find the value of $\tan \theta$.	[6]

the 1	shed to the midpoint of the string. The system is in equilibrium with P at a dismidpoint of AB .	tance $\frac{3}{2}a$ below
(a)	Find λ in terms of m and g .	

ind, in	terms of a	and g, th	e speed	of P as	it passes	through	M in th	e subseq	uent moti	ion.
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Find the value of	of u.				[5
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A ring of weight W, with radius a and centre O, is at rest on a rough surface that is inclined to the horizontal at an angle α where $\tan \alpha = \frac{1}{2}$. The plane of the ring is perpendicular to the inclined surface and parallel to a line of greatest slope of the surface. The point P on the circumference of the ring is such that OP is parallel to the surface.

A light inextensible string is attached to P and to the point Q, which is on the surface, such that PQ is horizontal (see diagram). The points O, P and Q are in the same vertical plane. The system is in limiting equilibrium and the coefficient of friction between the ring and the surface is μ .

Find, in terms of W , the tension in the string PQ .	[4]

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leng alor <i>B</i> is	o particles A and B of masses m and km respectively are connected by a light inextensible string of the a . The particles are placed on a rough horizontal circular turntable with the string taut and lying a radius of the turntable. Particle A is at a distance a from the centre of the turntable and partice at a distance a from the centre of the turntable. The coefficient of friction between each partice the turntable is $\frac{1}{5}$.
Wh	en the turntable is made to rotate with angular speed $\frac{2}{5}\sqrt{\frac{g}{a}}$, the system is in limiting equilibrium.
(a)	Find the tension in the string, in terms of m and g .

(b)	Find the value of k .	[3]
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	article P of mass 2 kg moving on a horizontal straight line has displacement x m in the line and velocity v m s ⁻¹ at time t s. The only horizontal force acting or $(v-1)^2 e^{-t}$ N and acts towards O . When $t=0$, $x=1$ and $v=3$.	
1)	Find an expression for v in terms of t .	
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wiie	re OQ makes an angle θ with the upward vertical through O .	
(a)	Show that $\cos \theta = \frac{u^2 + 2ag}{3ag}$.	[

It is given that $\cos \theta = \frac{5}{6}$.

Find, in terms of a and g , an expression for the vertical component of the velocity of P just hits the horizontal plane to which the sphere is fixed.	
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Find an expression for the time taken by P to fall from Q to the plane. Give your answ	er in
Find an expression for the time taken by P to fall from Q to the plane. Give your answ form $k\sqrt{\frac{a}{g}}$, stating the value of k correct to 3 significant figures.	er in
Find an expression for the time taken by P to fall from Q to the plane. Give your answ form $k\sqrt{\frac{a}{g}}$, stating the value of k correct to 3 significant figures.	ver in
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Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.								
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